On Carleson-type embeddings for Bergman spaces of harmonic functions

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Given a measure μ on a bounded domain $\Omega \subset \mathbb{R}^n$ with C^1 boundary we investigate the following problem: when is a weighted harmonic Bergman space $A^p_\alpha(\Omega)$ continuously embedded in weighted space $L^p(\Omega) = L^p(\mu, \Omega)$? We give a sufficient Carleson type condition for all $\alpha > -1$ and $0 < p < \infty$ which is also necessary for $p > 1 + \frac{\alpha+2}{n-2}$.

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