

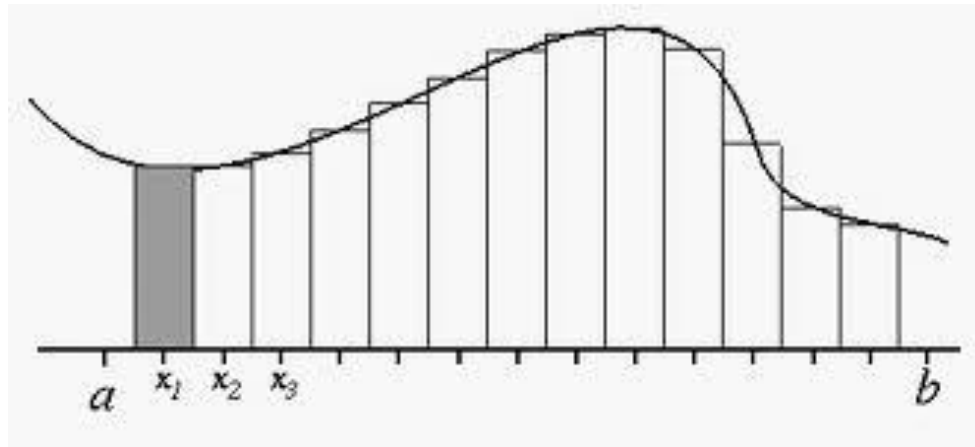
Parallel programming

MPI Interface

01 - π

The value of the definite integral $\int_0^1 \frac{4}{1+x^2} dx$ is π . We can use numerical integration to compute π by approximating the area under the curve $y = \frac{4}{1+x^2}$. A simple way to do this is called the rectangle rule (see below). We divide the interval $[0,1]$ into k subintervals of equal size. We find the height of the curve at the midpoint of each of these subintervals. With these heights we can construct k rectangles. The area of the rectangles approximates the area under the curve. As k increases, the accuracy of the estimate also increases.

Write a parallel program to compute π using the rectangle rule with 1,000,000 intervals.



02 - Simpson's rule

Simpson's rule is a better numerical integration algorithm than the rectangle rule because it converges more quickly. Suppose we want to compute $\int_a^b f(x) dx$. We divide the interval $[a, b]$ into n subintervals, where n is even. Let x_i denote the end of the i -th interval, for $1 \leq i \leq n$, and let x_0 denote the beginning of the first interval. According to Simpson's rule:

$$\int_a^b f(x) dx \approx \frac{1}{3n} \left[f(x_0) - f(x_n) + \sum_{i=1}^{n/2} (4f(x_{2i-1}) + 2f(x_{2i})) \right]$$

Write a parallel program to compute the value of π using Simpson's rule:

$$f(x) = \frac{4}{1+x^2}, a = 0, b = 1 \text{ and } n = 1,000,000,000.$$