

Definisanje tipova i klasa

Deklaracija tipa

Definisanje sinonima za tipove

```
type String = [Char]
```

```
type Pos = (Int,Int)
```

```
origin :: Pos
```

```
origin = (0,0)
```

```
left :: Pos -> Pos
```

```
left (x,y) = (x-1, y)
```

```
ghci> left (3,4)  
(2,4)
```

```
type Pair a = (a,a)
```

```
copy :: a -> Pair a
```

```
copy x = (x,x)
```

```
mult :: Pair Int -> Int
```

```
mult (m,n) = m*n
```

```
ghci> copy 3  
(3,3)
```

```
ghci> mult (3,4)  
12
```

Deklaracija tipa

Mogu biti ugnježdene

- Na osnovi jednog tipa može se definisati drugi

```
type Pos = (Int, Int)
type Trans = Pos -> Pos
```

Ne mogu biti rekurzivne

- Ovakvu definiciju nije moguće „razviti“

```
type Tree = (Int, [Tree])
```

Deklaracija tipa

Mogu biti sa parametrom

```
type Pair a = (a,a)
```

Mogu imati više parametara

```
type Assoc k v = [(k,v)]
```

```
find :: Eq k => k -> Assoc k v -> v  
find k t = head [v | (k',v) <- t, k == k']
```

Deklaracija podataka

Definicija novog tipa navođenjem vrednosti (konstruktora)

```
data Bool = False | True
```

Mogu se posmatrati kao kontekstno slobodne gramatike

```
data Answer = Yes | No | Unknown  
deriving (Show)
```

```
answers :: [Answer]  
answers = [Yes, No, Unknown]
```

```
flip' :: Answer -> Answer  
flip' Yes      = No  
flip' No       = Yes  
flip' Unknown = Unknown
```

```
ghci> flip' Yes  
  
<interactive>:5:1: error:  
  * No instance for (Show Answer) arising from a use of `print'  
  * In a stmt of an interactive GHCi command: print it  
ghci>
```

```
ghci> flip' Yes  
No  
.
```

Deklaracija podataka

```
data Move = North | South | East | West
deriving (Show)

move :: Move -> Pos -> Pos
move North (x,y) = (x,y+1)
move South (x,y) = (x,y-1)
move East (x,y) = (x+1,y)
move West (x,y) = (x-1,y)

moves :: [Move] -> Pos -> Pos
moves [] p = p
moves (m:ms) p = moves ms (move m p)
```

```
ghci> moves [North,North,West] (1,2)
(0,4)
```

Deklaracija podataka

```
data Shape = Circle Float | Rect Float Float

square :: Float -> Shape
square n = Rect n n

area :: Shape -> Float
area (Circle r) = pi * r^2
area (Rect x y) = x * y
```

```
ghci> :type Circle
Circle :: Float -> Shape
ghci> area (square 5)
25.0
```

Deklaracija podataka

U slučajevima kada se koriste „zaključane“ biblioteke u kojima se definisani neki tipovi podataka

- Jednostavno je definisati nove tipove na osnovu već definisanih
- Jednostavno je definisati nove metode za definisane tipove
- Problem predstavlja definisanje podtipa koji ne može da se doda „zaključanom“ tipu

`data Shape = ... | Polygon... !!!`

Deklaracija podataka sa parametrima

```
data Maybe a = Nothing | Just a
```

```
safediv :: Int -> Int -> Maybe Int
safediv _ 0 = Nothing
safediv m n = Just (m `div` n)
```

```
safehead :: [a] -> Maybe a
safehead [] = Nothing
safehead xs = Just (head xs)
```

```
ghci> safehead []
Nothing
ghci> safehead [2,3,4]
Just 2
```

Rekurzivni tipovi

```
data Nat = Zero | Succ Nat  
deriving (Show)  
  
nat2int :: Nat -> Int  
nat2int Zero = 0  
nat2int (Succ n) = 1 + nat2int n  
  
int2nat :: Int -> Nat  
int2nat 0 = Zero  
int2nat n = Succ (int2nat (n-1))
```

Peanovi brojevi

Kako bez Int definisati

add :: Nat -> Nat -> Nat

```
ghci> int2nat 4  
Succ (Succ (Succ (Succ Zero)))  
Nothing
```

Aritmetički izrazi

```
data Expr = Val Int  
          | Add Expr Expr  
          | Mul Expr Expr  
deriving (Show)
```

```
e1 :: Expr  
e1 = Add (Val 1) (Mul (Val 3) (Val 3))
```

```
size :: Expr -> Int  
size (Val n)    = 1  
size (Add x y) = size x + size y  
size (Mul x y) = size x + size y
```

```
eval :: Expr -> Int  
eval (Val n)    = n  
eval (Add x y) = eval x + eval y  
eval (Mul x y) = eval x * eval y
```

```
ghci> e1  
Add (Val 1) (Mul (Val 3) (Val 3))  
ghci> size e1  
3  
ghci> eval e1  
10
```

Kako bi za ovakav tip podataka bila definisana funkcija fold i kako bi se koristila?

Binarna stabla

```
data Tree a = Leaf a | Node (Tree a) a (Tree a)
```

```
occurs :: Eq a => a -> Tree a -> Bool
```

- Pojavljivanje čvora u stablu

```
flatten :: Tree a -> [a]
```

- Formiranje sortirane liste od stabla

Iskazne formule

```
data Prop = Const Bool  
          | Val Char  
          | Not Prop  
          | And Prop Prop  
          | Imply Prop Prop
```

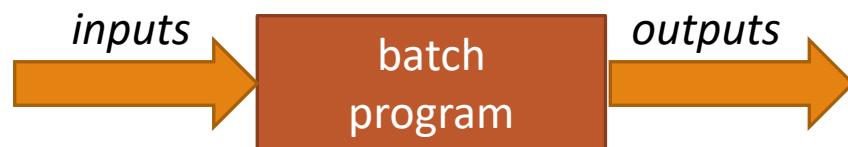
isTaut :: Prop -> Bool

- Ispitivanje da li je formula tutologija
 - eval – vrednost formule
 - vars – iskazna slova iz formule
 - bools – generisanje svih valuacija
 - subs – sve kombinacije vrednosti iskaznih slova i njihovih valuacija

```
bools :: Int -> [[Bool]]  
bools 0 = [[]]  
bools n = map (False:) bss ++ map (True:) bss  
          where bss = bools (n-1)
```

Interaktivni programi

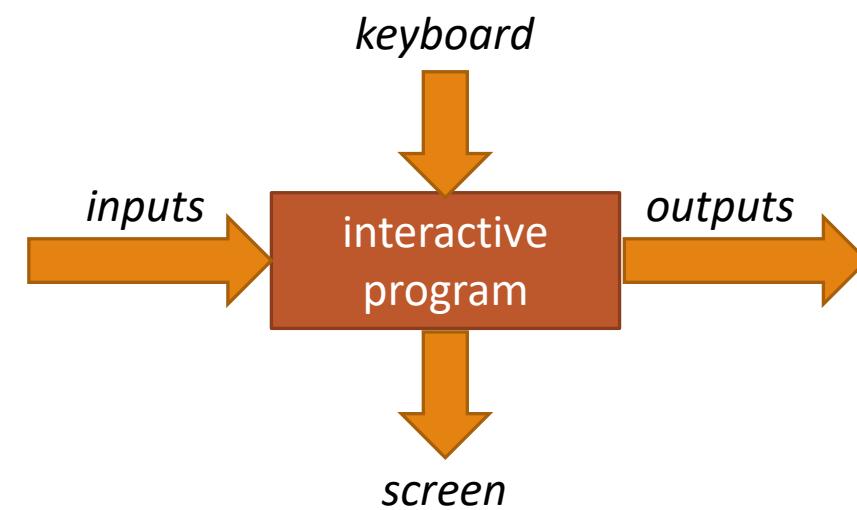
Uvod



Haskell programi su čisto funkcijski/matematički
No side effects

ReadLine – nije matematička funkcija
Interactive programs **have side effects**

Current “state of world” as argument



Tip IO

```
type IO = World -> World
```

```
type IO a = World -> (a, World)
```

IO a – akcija koja vraća tip a

- IO Char – vraća karakter
- IO () -- akcija koja ne vraća vrednost

Standardna biblioteka sadrži veliki broj IO akcija

- getChar :: IO Char <~> getChar :: () -> IO Char
- putChar :: Char -> IO ()
- return :: a -> IO a

Sekvence

Niz akcija koje se spajaju u jednu korišćenjem ključne reči **do**

```
do v1 <- a1  
    v2 <- a2  
    ...  
    vn <- an  
    return (f v1 v2 ... vn)
```

```
a :: IO (Char, Char)  
a = do x <- getChar  
       getChar  
       y <- getChar  
       return (x,y)
```

```
ghci> a  
a  
b  
('a','b')
```

Učitavanje i štampanje stringova

```
getLine :: IO String
getLine = do x <- getChar
            if x == '\n' then
                return []
            else
                do xs <- getLine
                   return (x:xs)

b :: IO String
b = do x <- getLine
       return x
```

```
ghci> b
Haskell
"Haskell"
```

Učitavanje i štampanje stringova

```
putStr      :: String -> IO ()  
putStr []    = return ()  
putStr (x:xs) = do putChar x  
                  putStr xs
```

```
putStrLn :: String -> IO ()  
putStrLn xs = do putStr xs  
                  putChar '\n'
```

```
ghci> putStrLn "abcd"  
abcdghci>
```

```
ghci> putStrLn "abcd"  
abcdghci>
```

Interaktivni program

```
strlen :: IO ()  
strlen = do putStrLn "Enter a string "  
           xs <- getLine  
           putStrLn "The string has "  
           putStrLn (show (length xs))  
           putStrLn " characters"
```

```
ghci> strlen  
Enter a string Haskell  
The string has 7 characters
```

Izračunavanje akcija izvršava „*side effects*“ dok je konačni rezultat zanemaren

Hangman

Top-down pristup

```
import System.IO
```

```
hangman :: IO ()  
hangman = do putStrLn "Think of a word:"  
            word <- getLine  
            putStrLn "Try to guess it:"  
            play word
```

```
*Main> hangman  
Think of a word:  
-----  
Try to guess it:  
?beograd  
-rag--e-a-  
?kragujevac  
You got it!
```

Hangman

Prihvatanje reči, ali bez prikazivanja karaktera

```
sgetLine :: IO String
sgetLine = do x <- getCh
             if x == '\n' then
               do putChar x
                  return []
             else
               do putChar '-'
                  xs <- sgetLine
                  return (x:xs)
```

Hangman

Prihvatanje karaktera, bez prikazivanja

```
getCh :: IO Char
getCh = do hSetEcho stdin False
          x <- getChar
          hSetEcho stdin True
          return x
```

Hangman

Glavna petlja

```
play :: String -> IO ()  
play word = do putStrLn "?"  
              guess <- getLine  
              if guess == word then  
                putStrLn "You got it!"  
              else  
                do putStrLn (match word guess)  
                play word
```

```
match :: String -> String -> String  
match xs ys = [if elem x ys then x else '-' | x <- xs]
```

Kako proširiti brojačem pokušaja?

Monadi i ostalo

Funktori

Uopštenje funkcije map

Ideja mapiranja funkcija na svaki element ne mora biti ograničena na liste

```
map :: (a -> b) -> [a] -> [b]
map f xs = [f x | x <- xs]
```

Funktori – klasa tipova koji podržavaju upšteno mapiranja

```
class Functor f where
    fmap :: (a -> b) -> f a -> f b
```

fmap prihvata funkciju $a \rightarrow b$ i na strukturu tipa $f\ a$, čiji su elementi tipa a , primjenjuje funkciju i vraća strukturu tipa $f\ b$

f mora biti parametrizovan tip

Funktori

```
instance Functor [] where
-- fmap :: (a -> b) -> [a] -> [b]
fmap = map
```

```
instance Functor Maybe where
-- fmap :: (a -> b) -> Maybe a -> Maybe b
fmap _ Nothing = Nothing
fmap g (Just x) = Just (g x)
```

```
ghci> map (+1) [1,3,4,7]
[2,4,5,8]
ghci> fmap (+1) [1,3,4,7]
[2,4,5,8]
```

```
ghci> fmap (+1) Nothing
Nothing
ghci> fmap (^2) (Just 3)
Just 9
ghci> fmap not (Just False)
Just True
```

```
ghci> fmap (++"!") getLine
hi
"hi!"
```

Funktori

```
data Tree a = Leaf a | Node (Tree a) (Tree a)
    deriving Show

instance Functor Tree where
    -- fmap :: (a -> b) -> Tree a -> Tree b
        fmap f (Leaf x) = Leaf (f x)
        fmap f (Node left right) = Node (fmap f left) (fmap f right)
```

```
ghci> fmap length (Leaf "abc")
Leaf 3
ghci> fmap even (Node (Leaf 1) (Leaf 2))
Node (Leaf False) (Leaf True)
ghci> fmap (\x -> x*x) (Node (Leaf 1) (Leaf 2))
Node (Leaf 2) (Leaf 4)
```

Zakoni za funkture

fmap id = id

fmap (g.h) = fmap g . fmap h

```
| ghci> fmap (not.even) [1,2]
| [True, False]
| ghci> (fmap not . fmap even) [1,2]
| [True, False]
```

Aplikativni funktori - Applicatives

Uopštenje funktora na funkcije sa više argumenata

Definisati hijerarhiju za fmap, npr.

```
fmap0 :: a -> f a
fmap1 :: (a -> b) -> f a -> f b
fmap2 :: (a -> b -> c) -> f a -> f b -> f c
fmap3 :: (a -> b -> c -> d) -> f a -> f b -> f c -> f d
...
```

Ili **curring**

```
pure :: a -> f a
(<*>) :: f (a -> b) -> f a -> f b
```

pure – konvertuje tip a u tip f a

<*> - uopšten oblik primene funkcije gde su funkcija argument, vrednosti argumenta i vrednost rezultata su f strukture

Aplikativni funktori - Applicatives

pure $g \text{ } (*> \text{ } x_1 \text{ } (*> \text{ } x_2 \text{ } (*> \dots \text{ } (*> \text{ } x_n$

Svaki argument x_i ima tip $f \text{ } a_i$, a rezultat je tipa $f \text{ } b$

```
fmap0 :: a -> f a
fmap0 = pure

fmap1 :: (a -> b) -> f a -> f b
fmap1 g x = pure g (*> x

fmap2 :: (a -> b -> c) -> f a -> f b -> f c
fmap2 g x y = pure g (*> x (*> y

fmap3 :: (a -> b -> c -> d) -> f a -> f b -> f c -> f d
fmap3 g x y z = pure g (*> x (*> y (*> z

...
```

```
class Functor f => Applicative f where
    pure :: a -> f a
    (*>) :: f (a -> b) -> f a -> f b
```

Aplikativni funktori - Applicatives

Klasa funktora koja podržava pure i `<*>` naziva se aplikativni funktor

```
class Functor f => Applicative f where
    pure :: a -> f a
    (<*>) :: f (a -> b) -> f a -> f b
```

```
ghci> pure (+1) <*> Just 1
Just 2
ghci> pure (+) <*> Just 1 <*> Just 2
Just 3
ghci> pure (+) <*> Nothing <*> Just 2
Nothing
```

```
ghci> pure (\x -> \y -> \z -> x*y*z) <*> Just 1 <*> Just 2 <*> Just 3
Just 6
```

```
ghci> pure (*) <*> [1,2] <*> [3,4]
[3,4,6,8]
```

Aplikativni zakoni

```
pure id <*> x    = x
pure (g x)        = pure g <*> pure x
x <*> pure y     = pure (\g -> g y) <*> x
x <*> (y <*> z) = (pure (.) <*> x <*> y) <*> z
```

Monadi

```
data Expr = Val Int | Div Expr Expr
eval :: Expr -> Int
eval (Val n)  = n
eval (Div x y) = eval x `div` eval y
```

```
eval :: Expr -> Maybe Int
eval (Val n) = Just n
eval (Div x y) = case eval x of
    Nothing -> Nothing
    Just n -> case eval y of
        Nothing -> Nothing
        Just m -> safediv n m
```

```
ghci> eval (Div (Val 1) (Val 0))
*** Exception: divide by zero
```

```
safediv :: Int -> Int -> Maybe Int
safediv _ 0 = Nothing
safediv n m = Just (n `div` m)
```

```
ghci> eval (Div (Val 1) (Val 0))
Nothing
```

Monadi

Rešenje preko aplikativnih funktora?

```
eval :: Expr -> Maybe Int  
eval (Val n) = pure n  
eval (Div x y) = pure safediv <*> eval x <*> eval y
```

Neodgovarajući tipovi!!!

```
(>>=) :: m a -> (a -> m b) -> m b  
mx >>= f = case mx of  
    Nothing -> Nothing  
    Just x -> f x
```

```
eval :: Expr -> Maybe Int  
eval (Val n) = Just n  
eval (Div x y) = eval x >>= \n ->  
    eval y >>= \m ->  
    safediv n m
```

Monadi

Uopšten oblik

```
m1 >>= \x1 ->  
m2 >>= \x2 ->  
...  
mn >>= \xn ->  
f x1 x2 ... xn
```

```
class Applicative m => Monad m where  
    return :: a -> m a  
    (=>) :: m a -> (a -> m b) -> m b  
  
    return = pure
```

IO akcije, funkcije nad stablima, izrazima, do notacija, Maybe, ...

Zakoni za monade

```
return x >>= f      = f x
```

```
mx >>= return      = mx
```

```
(mx >>= f) >>= g  = mx >>= (\x -> (f x >>=g))
```

Tipovi i klase tipova

Type	Typeclasses
Bool	Eq, Ord, Show, Read, Enum, Bounded
Char	Eq, Ord, Show, Read, Enum, Bounded
Int	Eq, Ord, Show, Read, Enum, Bounded, Num, Real, Integral
Integer	Eq, Ord, Show, Read, Enum, Num, Real, Integral
Float	Eq, Ord, Show, Read, Enum, Num, Real, Fractional, RealFrac, Floating, RealFloat
Double	Eq, Ord, Show, Read, Enum, Num, Real, Fractional, RealFrac, Floating, RealFloat
Word	Eq, Ord, Show, Read, Enum, Bounded, Num, Real, Integral
Ordering	Eq, Ord, Show, Read, Enum, Bounded, Semigroup, Monoid
()	Eq, Ord, Show, Read, Enum, Bounded, Semigroup, Monoid
Maybe a	Eq, Ord, Show, Read, Semigroup, Monoid, Functor, Applicative, Monad, Foldable, Traversable
[a]	Eq, Ord, Show, Read, Semigroup, Monoid, Functor, Applicative, Monad, Foldable, Traversable
(a,b)	Eq, Ord, Show, Read, Bounded, Semigroup, Monoid, Functor, Applicative, Monad, Foldable, Traversable
a->b	Semigroup, Monoid, Functor, Applicative, Monad
IO	Semigroup, Monoid, Functor, Applicative, Monad
IOError	Eq, Show