

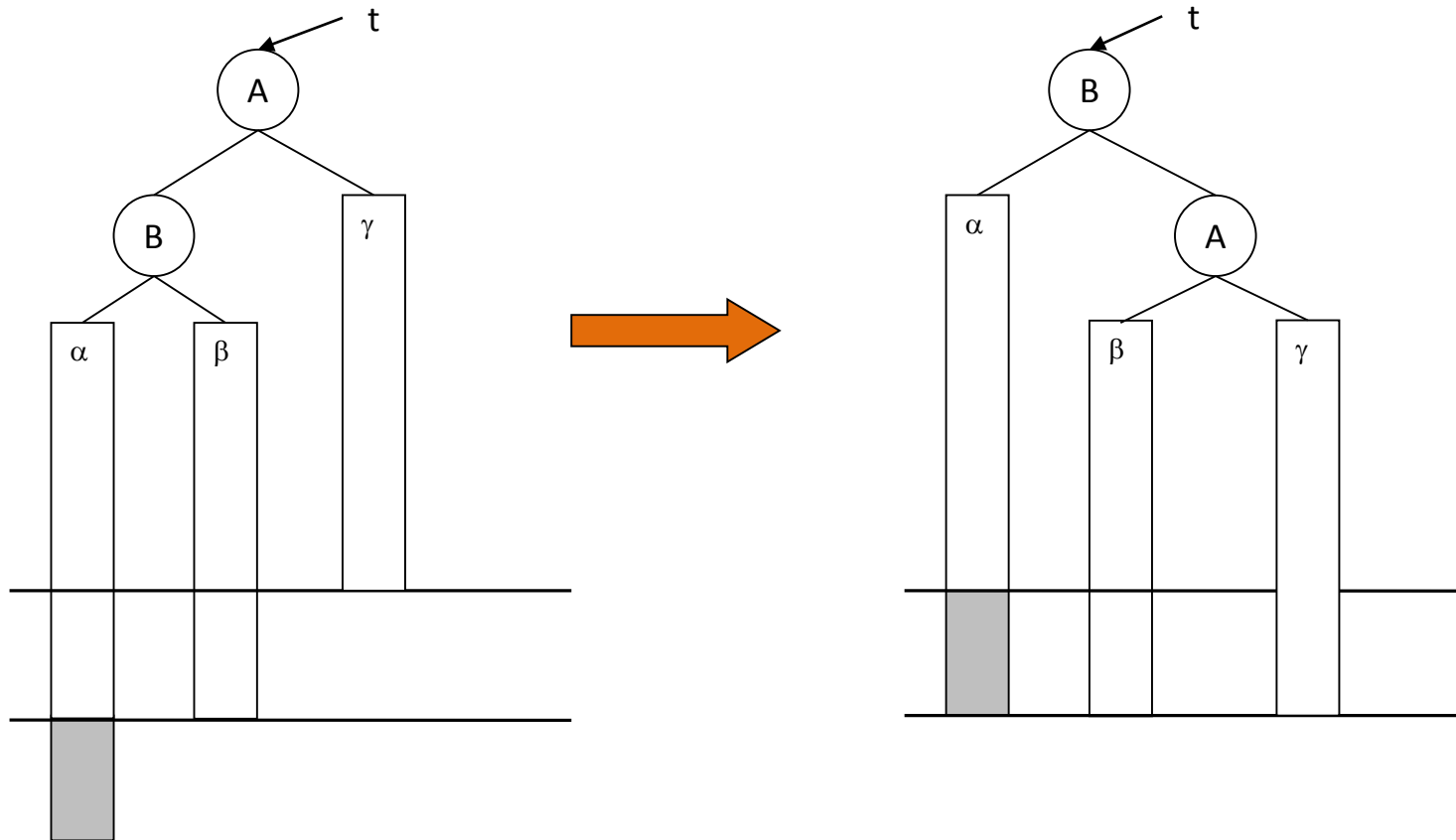
Binarna stabla

SPA2

Napisati program koji formira balansirano uređeno binarno stablo celih brojeva.

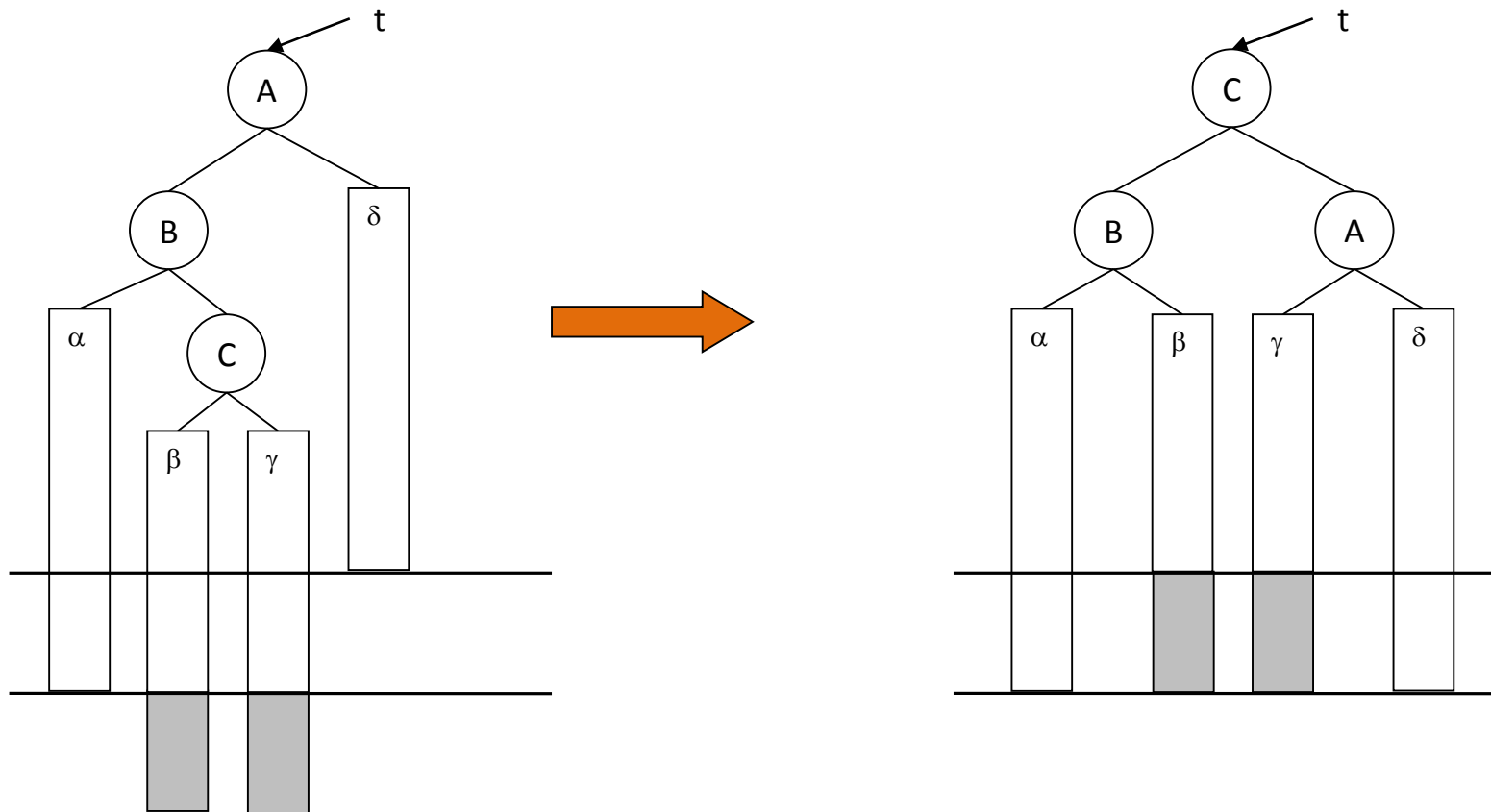
AVL-stabla (G.M. Adelson-Velsky and E.M. Landis)

$(t \rightarrow \text{balans} < -1) \ \&\& \ (t \rightarrow \text{levi} \rightarrow \text{balans} < 0)$



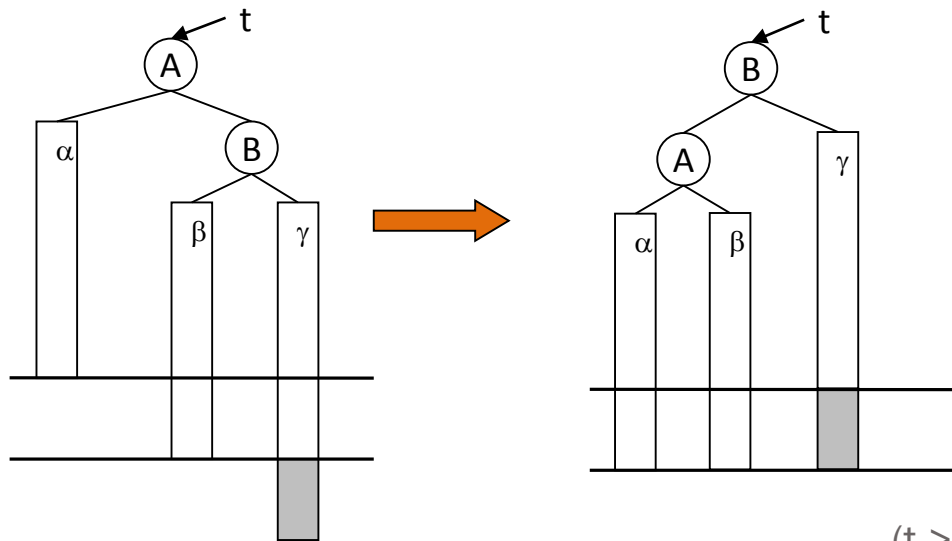
Desna rotacija

$(t \rightarrow \text{balans} < -1) \ \&\& \ !(t \rightarrow \text{levi} \rightarrow \text{balans} < 0)$



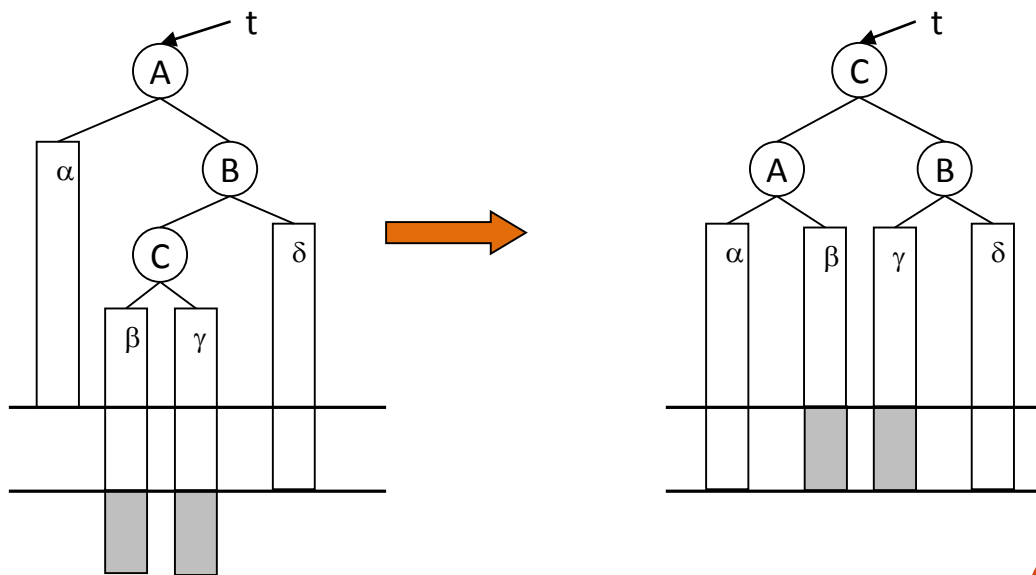
Dvostruka desna rotacija

$(t \rightarrow \text{balans} > 1) \ \&\& \ (t \rightarrow \text{desni} \rightarrow \text{balans} > 0)$



Leva rotacija

$(t \rightarrow \text{balans} > 1) \ \&\& \ !(t \rightarrow \text{desni} \rightarrow \text{balans} > 0)$



Dvostruka leva rotacija

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
struct drvo{
    int broj;
    int balans;
    struct drvo *levi,*desni;
};
#define novi(x) x=(struct drvo *) malloc(sizeof(struct drvo))

int dodaj(struct drvo **,int);
struct drvo* form();
void ispisi(struct drvo*);
void lrotacija(struct drvo**);
void drotacija(struct drvo**);
int dubina(struct drvo*);
int balansirano(struct drvo*);
```

```
main(){
    struct drvo *p,*q;
    p=form();
    ispis(p); printf("\n");
    printf("Dubina je %d\n",dubina(p));
    if (balansirano(p)) printf("jeste balansirano\n");
    else printf("nije balansirano\n");
}

struct drvo* form(){
    struct drvo *koren;
    int k;
    koren=NULL;
    scanf("%d",&k);
    while(k) {
        dodaj(&koren,k);
        scanf("%d",&k);
    }
    return koren;
}
```

```
void lrotacija(struct drvo **t){
```

```
    struct drvo *poml,*pomd;
```

```
    int stari_balans;
```

```
    poml = *t;
```

```
    pomd = poml->desni;
```

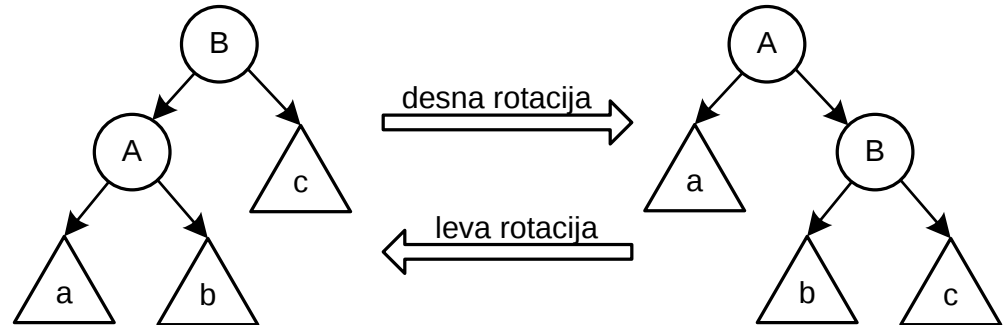
```
    poml->desni = pomd->levi;
```

```
    pomd->levi = poml;
```

```
    *t=pomd;
```

```
    poml->balans=dubina(poml->desni)-dubina(poml->levi);
```

```
    pomd->balans=dubina(pomd->desni)-dubina(pomd->levi);}
}
```



```
void drotacija(struct drvo **t){
```

```
    struct drvo *poml,*pomd;
```

```
    int stari_balans;
```

```
    pomd = *t;
```

```
    poml = pomd->levi;
```

```
    pomd->levi = poml->desni;
```

```
    poml->desni = pomd;
```

```
    *t=poml;
```

```
    poml->balans=dubina(poml->desni)-dubina(poml->levi);
```

```
    pomd->balans=dubina(pomd->desni)-dubina(pomd->levi);}
}
```

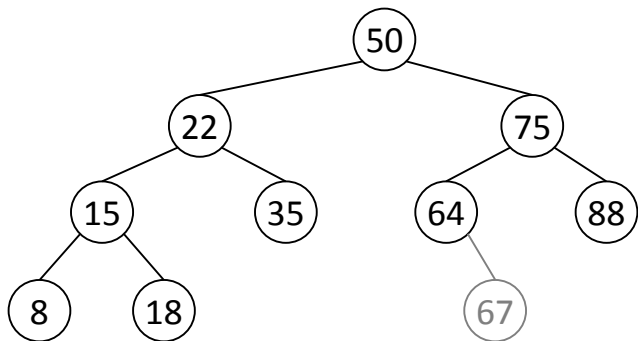
```
int dodaj(struct drvo **p, int vrednost){
    int inkrement, rezultat;
    struct drvo *t = *p;
    rezultat = 0;
    if(t==NULL){
        novi(t);
        if(t==NULL){
            printf("Greska pri alociranju memorije\n");
            exit(0);
        }
        t->broj = vrednost;
        t->levi = t->desni = NULL;
        t->balans = 0;
        rezultat = 1;
    }
    ...
}
```

...

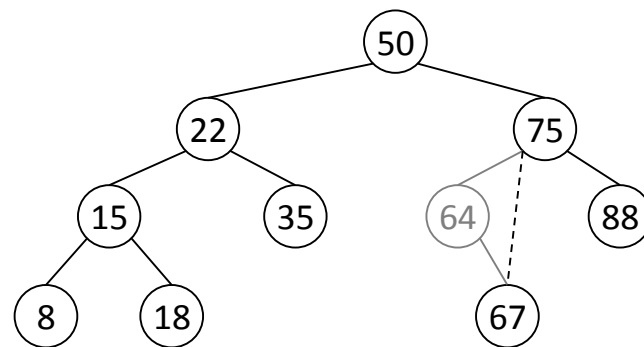
```
else{
    if(vrednost > t->broj) inkrement=dodaj(&(t->desni),vrednost);
    else inkrement=-dodaj(&(t->levi),vrednost);
    t->balans += inkrement;
    if(inkrement!=0 && t->balans!=0){
        if(t->balans<-1 ){
            if(t->levi->balans<0) drotacija(&t);
            else{ lrotacija(&(t->levi)); drotacija(&t); }
        }
        else if(t->balans>1){
            if(t->desni->balans>0 ) lrotacija(&t);
            else{ drotacija(&(t->desni)); lrotacija(&t); }
        }
        else rezultat = 1;
    }
}
*p = t;
return rezultat;
}
```

Brisanje čvora iz stabla

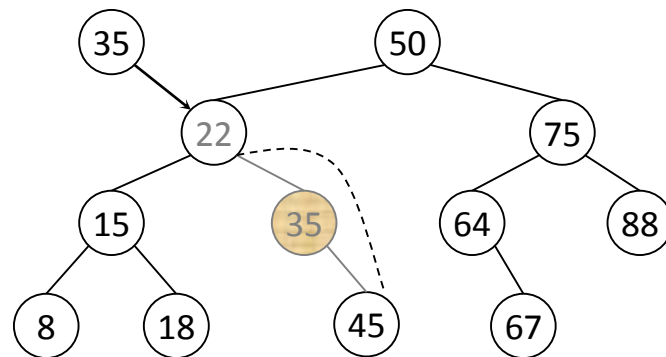
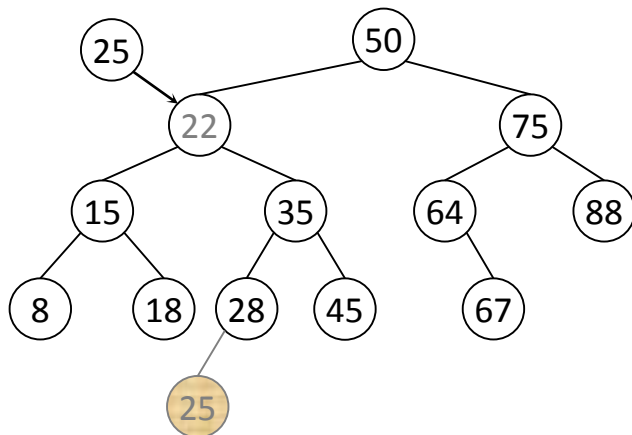
Čvor bez naslednika:



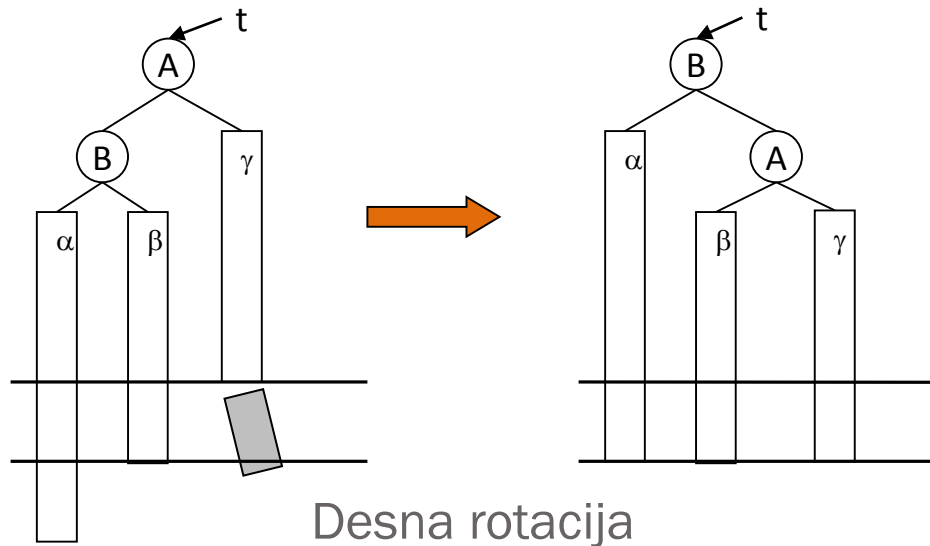
Čvor sa jednim naslednikom:



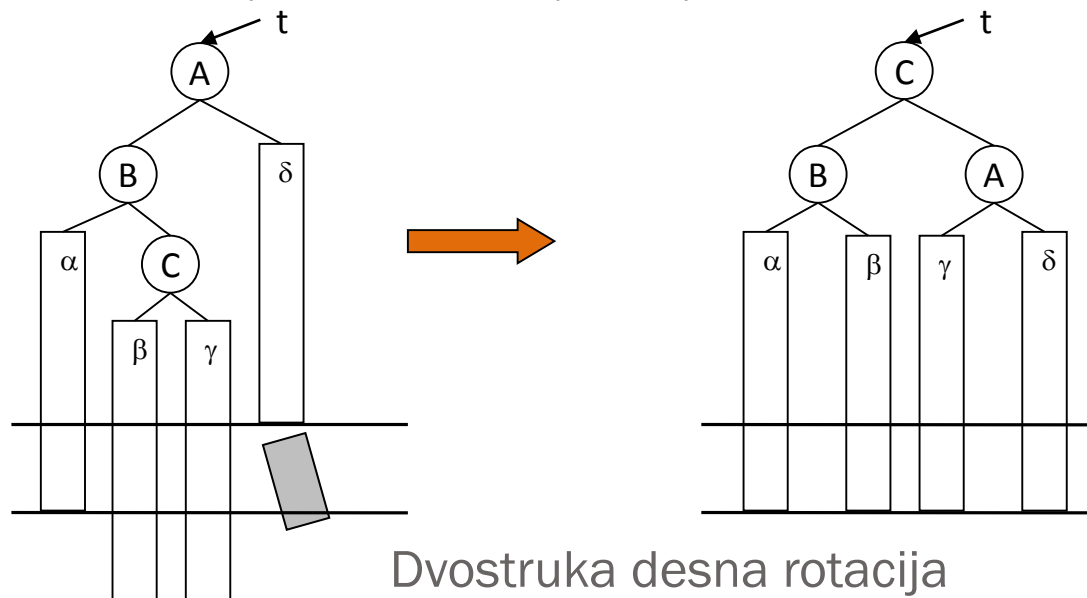
Čvor sa dva naslednika:



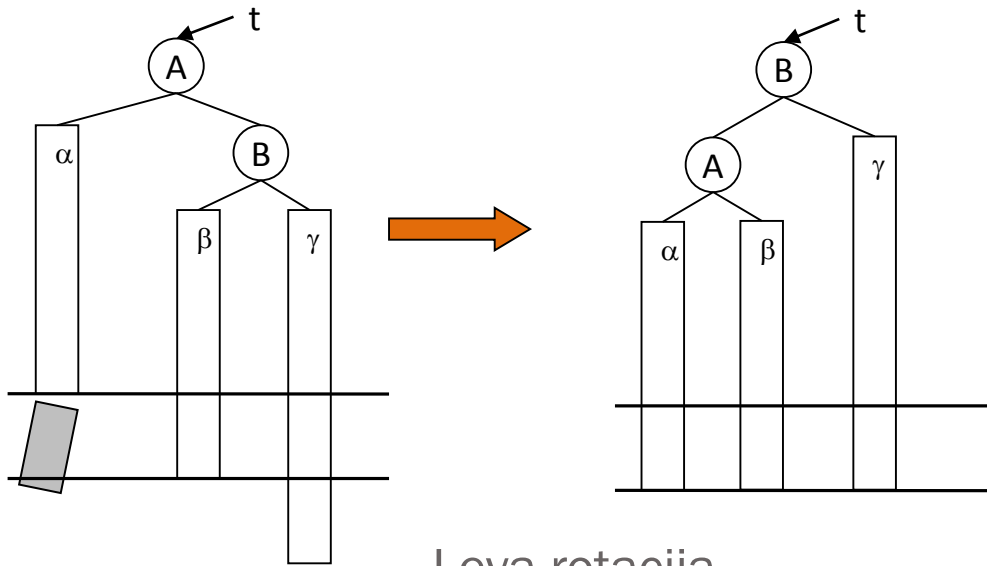
$(t \rightarrow \text{balans} < -1) \ \&\& \ (t \rightarrow \text{levi} \rightarrow \text{balans} < 0)$



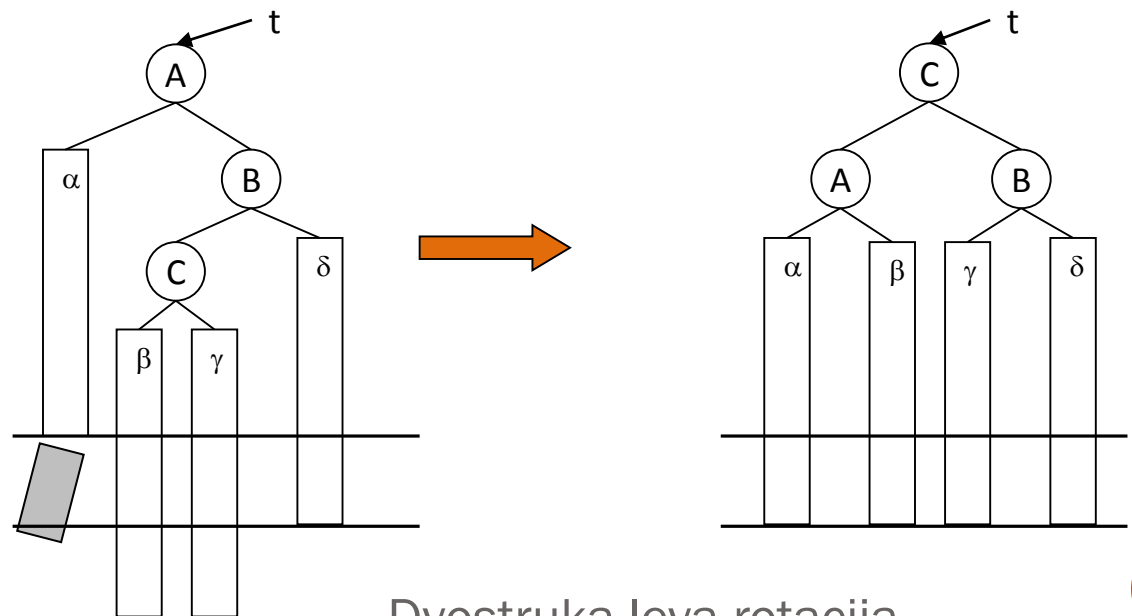
$(t \rightarrow \text{balans} < -1) \ \&\& \ !(t \rightarrow \text{levi} \rightarrow \text{balans} < 0)$



$(t \rightarrow \text{balans} > 1) \ \&\& \ (t \rightarrow \text{desni} \rightarrow \text{balans} > 0)$



$(t \rightarrow \text{balans} > 1) \ \&\& \ !(t \rightarrow \text{desni} \rightarrow \text{balans} > 0)$



Napisati program koji iz formiranog uređenog balansiranog binarnog stabla briše čvor čija je vrednost jednaka unetom broju **K**.

```
int nadji(struct drvo **p){
    struct drvo *pom,*pom1;
    int rez;
    pom=*p;
    if (!pom->levi) {
        rez=pom->broj;
        pom=pom->desni;
    }
    else rez=nadji(&(pom->levi));
    if (pom) {
        pom->balans=dubina(pom->desni)-dubina(pom->levi);
        sredi(&pom);
    }
    *p=pom;
    return rez;
}
```

```

void sredi(struct drvo **p){
    struct drvo *t;
    if(*p){
        t=*p;
        if( t->balans<-1 ){
            if( t->levi->balans<0 ) drotacija(&t);
            else{
                lrotacija(&(t->levi)); drotacija(&t);
            }
        }
        else if( t->balans>1 ){
            if( t->desni->balans>0 ) lrotacija(&t);
            else{
                drotacija(&(t->desni)); lrotacija(&t);
            }
        }
        *p=t;
    }
}

```

```
struct drvo* obrisi_b(struct drvo *p,int k){
    struct drvo *pom;
    if(!p) return NULL;
    if (p->broj==k) {
        if((!p->levi) && (!p->desni)) {
            free(p);
            return NULL;
        }
        if((!p->levi) && (p->desni)) {
            pom=p->desni;
            free(p);
            return pom;
        }
        if((p->levi) && (!p->desni)){
            pom=p->levi;
            free(p);
            return pom;
        }
    }
}
```

...

```
...  
    if((p->levi) && (p->desni)){  
        p->broj=nadji(&(p->desni));  
        p->balans=dubina(p->desni)-dubina(p->levi);  
        sredi(&p);  
        return p;  
    }  
}  
if(k<p->broj){  
    p->levi=obrisi_b(p->levi,k);  
    p->balans=dubina(p->desni)-dubina(p->levi);  
    sredi(&p);  
    return p;  
}  
else{  
    p->desni=obrisi_b(p->desni,k);  
    p->balans=dubina(p->desni)-dubina(p->levi);  
    sredi(&p);  
    return p;  
}  
}
```